

CBCS SCHEME

USN 1 A M 2 0 M T 4 0 7

18MT34

Third Semester B.E. Degree Examination, July/August 2021 Control Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions.

1. a. Compare open loop and closed loop control system. (10 Marks)
 b. For the Fig Q1(b) shown below, determine TF $\frac{x_2(s)}{x_1(s)}$.

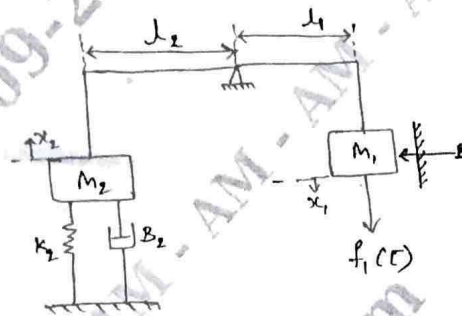


Fig Q1(b)

(10 Marks)

2. a. Draw the analogous circuits using F-V and F-I analogy for the mechanical system shown below Fig Q2(a)

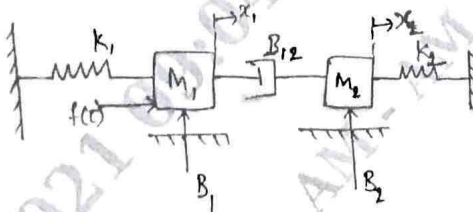


Fig Q2(a)

(12 Marks)

- b. Obtain $\frac{C(s)}{R(s)}$ using Block diagram reduction rules for the Fig Q2(b) shown below :

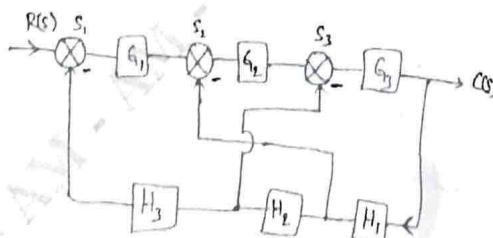


Fig Q2(b)

(08 Marks)

3. a. Construct the SFG for the set of system equations : $y_2 = G_1 y_1 + G_3 y_3$; $y_3 = G_4 y_1 + G_2 y_2 + G_5 y_3$; $y_4 = G_6 y_2 + G_7 y_3$ where y_4 is output

Find transfer function.

$\frac{y_4}{y_1}$

Using Maron's Gain formula

(10 Marks)

Important Note 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

- b. For the SFG shown in Fig Q3(b) below, find $\frac{C(s)}{R(s)}$ by Maron's Gain Formula.

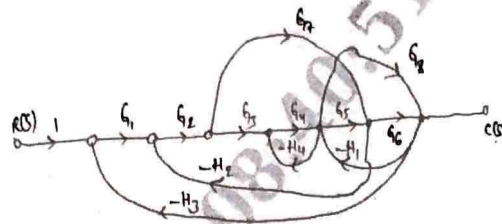


Fig Q3(b)

(10 Marks)

- 4 a. With a neat output versus time graph define the following: i) Delay Time (t_d) ii) Rise time (t_r) iii) Peak time (t_p) iv) Maximum overshoot (M_p) (10 Marks)

- b. For a system having $G(s) = \frac{15}{(s+1)(s+3)}$, $H(s) = 1$. Determine :

- i) Characteristics equation ii) ω_n and ξ [natural frequency and damping factor]
 iii) Time at which first undershoot will occur iv) Time period of oscillations related to ω_d
 v) Number of cycles output will perform before setting down for $\pm 2\%$ tolerance. (10 Marks)
- 5 a. Define the following : i) Absolute stability ii) Relative stability iii) Conditionally stable iv) Marginally stable. (04 Marks)

- b. For unity feedback system $G(s) = \frac{k}{s(1+0.4s)(1+0.25s)}$ find the range of values of k , marginal value k and frequency of oscillation (ω). (08 Marks)

- c. For a system with C.E - characteristics equation $F(s) = s^6 + 3s^5 + 4s^4 + 6s^3 + 5s^2 + 3s + 2 = 0$. Examine stability. (08 Marks)

- 6 a. State the advantages and limitation of frequency domain approach. (08 Marks)
 b. Explicitly discuss the correlation between time and frequency response of a second order system. Obtain the expression for resonant peak. (12 Marks)

- 7 Draw the appropriate root locus diagram for the closed loop system whose transfer function is given by $G(s)$. $H(s) = \frac{k}{s(s+2)(s^2+6s+25)}$ comment on stability. (20 Marks)

- 8 Sketch Bode plot for the transfer function $G(s) = \frac{k.s^2}{(1+0.25s)(1+0.025s)}$. Determine value of 'k' for gain cross over frequency to be 5 rad s^{-1} . (20 Marks)

- 9 a. Define : i) State variable ii) State vector iii) State space iv) State trajectory. (08 Marks)
 b. List the advantages of state variable analysis. (05 Marks)

- c. Obtain the transfer function : If $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -5 & -1 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 2 \\ 5 \end{bmatrix} u$ $y = [12] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ (07 Marks)

- 10 a. List the properties of state transition matrix and write the equation for transfer function from state model. (10 Marks)

- b. Consider a control system with state model

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u; \begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} u = \text{unit step. Compute the state transfer matrix and there from find the state response i.e., } x(t)$$

(10 Marks)